CPS 5310 Spring 2015 Mathematical and Computer Modeling Shirley Moore, Instructor January 22 Class

## **Introduction to Maxima with Examples**

One of the software packages we will use to do mathematical modeling in this course is Maxima. Maxima is a computer program for doing mathematical calculations, symbolic manipulations, numerical computations and graphics. You should install Maxima on your own computer and bring it to class. See the Maxima homepage at <a href="http://maxima.sourceforge.net/">http://maxima.sourceforge.net/</a> for more information. See also Ted Woollett's Maxima by Example available at <a href="http://www.csulb.edu/~woollett/">http://www.csulb.edu/~woollett/</a>.

Next let's try some of the simple modeling examples from Chapter 1 in the textbook. Before starting, you'll need to download and unpack the book software file MMS-V2.zip from <a href="https://sites.google.com/site/booksoftwaremms/">https://sites.google.com/site/booksoftwaremms/</a>.

**Example Problem 1**. Consider the problem of minimizing the metal used to construct a cylindrical tin having a volume of 1 liter. The following mathematical model can be used to solve the problem:

$$M = {\pi r^2 h = 1, A = 2\pi r^2 + 2\pi r h \rightarrow \min}$$

where r and h denote the radius and height of the cylinder, respectively. The first mathematical statement expresses the fact that the volume of the tin is 1 liter. The second statement requires the surface area of the tin to be minimized.

- 1a. Substitute the first equation into the second to obtain a function A(r) to be minimized.
- 1b. Explain how to use calculus to solve the problem.
- 1c. Examine the file Tin.mac from the Principles subfolder in the mms book software folder to see how it solves the problem.
- 1d. Use Maxima to run the batch file Tin.mac to obtain the solution to the problem. Explain the results.

**Example Problem 2**. What volumes of fluids A and B should be mixed to obtain 150 l of a fluid C that contains 70  $gl^{-1}$  of a substance, if A and B contain 50  $gl^{-1}$  and 80  $gl^{-1}$ , respectively.

- 2a. Determine the unknowns.
- 2b. Give precise definitions of the unknowns, including units.
- 2c. Translate the information in the problem description into mathematical statements.
- 2d. Examine the file Mix.mac to see how it solves the problem.
- 2e. Run the batch file Mix.mac in Maxima to obtain the solution to the problem.

**Example Problem 3**. Suppose the fluids A, B, C, and D contain concentration (in grams per liter) of the substances  $S_1$ ,  $S_2$ , and  $S_3$  as shown in the table below. What is the concentration

of  $S_3$  in a mixture of these fluids that contains 75% (percent by volume) of fluids A and B and that contains 4  $gl^{-1}$  and 5  $gl^{-1}$  of the substances  $S_1$  and  $S_2$ , respectively.

	A	В	С	D
$S_1$	2.5	8.2	6.4	12.7
$S_2$	3.2	15.1	13.2	0.4
$S_3$	1.1	0.9	2.2	3.1

- 3a. Determine and give a precise definition of the unknown(s).
- 3b. Translate the problem description into a mathematical model consisting of a system of linear equations. (Hint: To do this, you will need to introduce some auxiliary variables).
- 3c. Examine the file Mix1.mac to see how it solves the problem.
- 3d. Run the batch file Mix1.mac in Maxima to obtain the solution to the problem.

**Example Problem 4.** Suppose a farmer has a piece of farm land A square kilometers large to be planted with either wheat or barley or some combination of the two. Furthermore, suppose the farmer has a limited permissible amount F of fertilizer and P of insecticide that can be used, each of which is required in different amounts per unit area for wheat  $(F_1, P_1)$  and barley  $(F_2, P_2)$ . Let  $S_1$  be the selling price of wheat, and  $S_2$  the selling price of barley. How many square kilometers should be planted of wheat versus barley to maximize the revenue?

- 4a. Determine and give a precise definition of the unknowns.
- 4b. Formulate the problem as a mathematical model in the form of a linear programming problem.
- 4c. Examine the file Farm.mac to see how it solves the problem.
- 4d. Run the batch file Farm.mac from Maxima to obtain the solution to the problem.

**Preparation for next class**: Work through the Tank Labeling Problem in section 1.5.4.2, including running the file Label.mac in Maxima to obtain the solution.